

## Some AP-like Review Questions

$f(x)$  is a continuous function such that  $\int_a^b f(x) dx = 6$  and  $\int_c^a f(x) dx = 10$ .

Therefore,  $\int_b^c f(x) dx =$

- A) -16      B) -4      C) 0      D) 4      E) 16

$$\int_0^{\frac{\pi}{3}} \cos x dx$$

- A)  $\frac{1}{2}$       B)  $1 - \frac{\sqrt{3}}{2}$       C)  $\frac{\sqrt{3}}{2} - 1$       D)  $-\frac{\sqrt{3}}{2}$       E)  $\frac{\sqrt{3}}{2}$

14. From Salas, Hille, Etgen:

Let  $F(x) = 2x + \int_0^x \frac{\sin(2t)}{1+t^2} dt$ . Determine: (a)  $F(0)$ , (b)  $F'(0)$ , (c)  $F''(0)$ .

Find  $F'(x)$  given:

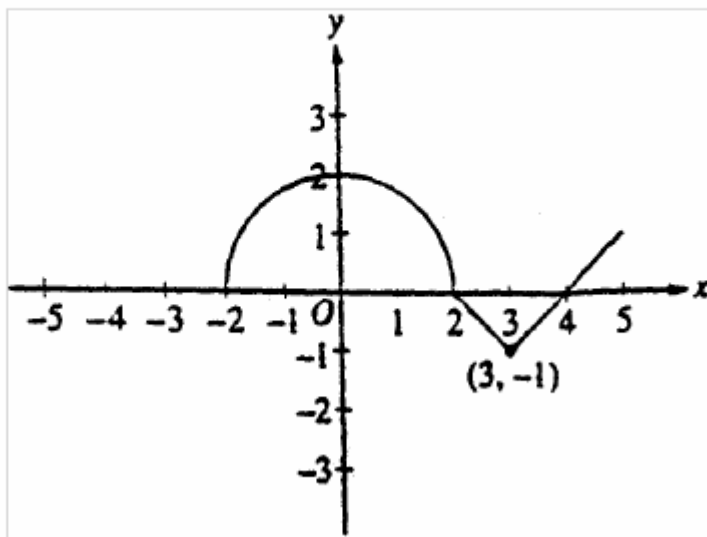
$$(a) F(x) = \int_x^5 3t \sin t dt$$

$$(b) F(x) = \int_0^{3x} \frac{1}{t^4 + 1} dt$$

$$(c) F(x) = \int_{2x}^{x^2} \frac{1}{2 + e^t} dt$$

From: Houston ACT webpage

1997 AB/BC 5 Free Response:



The graph of a function  $f$  consists of a semicircle and two line segments as shown above.

Let  $g$  be the function given by  $g(x) = \int_0^x f(t) dt$ .

- (a) Find  $g(3)$ .
- (b) Find all values of  $x$  on the open interval  $(-2, 5)$  at which  $g$  has a relative maximum. Justify your answer.
- (c) Write an equation for the line tangent to the graph of  $g$  at  $x = 3$ .
- (d) Find the  $x$ -coordinate of each point of inflection of the graph of  $g$  on the open interval  $(-2, 5)$ . Justify your answer.