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1. Find the equation of the tangent line to the curve  $x^2 + y^2 = 169$  at the point  $(5, -12)$
  
  
  
  
  
  
  
  
  
  
2. Find the equation of the tangent line to the curve  $f(x) = \sqrt{3\sin x + 9}$  at  $x = 0$

3. Let  $f$  be the function given by  $f(x) = \tan x$  and let  $g(x) = x^2$ . At what value of  $x$  in the interval  $0 \leq x \leq \pi$  do the graphs of  $f$  and  $g$  have parallel tangent lines?  
[Calculator permitted for this question]

4.. Consider the differential equation  $\frac{dy}{dx} = \frac{x}{y}$  where  $y \neq 0$ . Write the equation of the tangent line to the solution curve that passes through the point  $(3, -1)$  and use it to approximate  $f(2.9)$

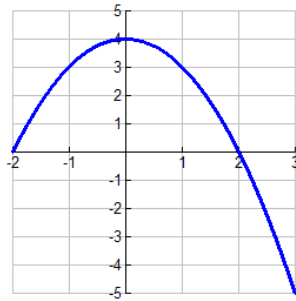
5. Consider the curve  $x^2 + y^2 = 25$  for  $y \geq 0$

(a) Find  $\frac{dy}{dx}$

(b) Write the equation of the tangent line to the curve at  $x = 3$

(c) Find the point on the curve where the tangent line is horizontal.

6. The graph of  $f(x) = 4 - x^2$  on the closed interval  $[-2, 3]$  is shown below.



- (a) Draw in the secant line from  $x = -2$  to  $x = 3$  and find the equation of the secant line [the average rate of change]
- (b) Find the value of  $c$ ,  $-2 < c < 3$ , that is guaranteed by the Mean Value Theorem. [First write the MVT statement] Then draw in the appropriate tangent line and find the tangent line equation.

7. Let  $f$  be the function given by  $f(x) = x^3 - 6x^2 + 7x + 3$ . Write the equation of the tangent line to the graph at  $x = 4$  and use it to approximate  $f(4.2)$

8. 2009AB5 [non-calculator]

$x$	2	3	5	8	13
$f(x)$	1	4	-2	3	6

Let  $f$  be a function that is twice differentiable for all real numbers. The table above gives values of  $f$  for selected points in the closed interval  $2 \leq x \leq 13$ .

(a) Estimate  $f'(4)$ . Show the work that leads to your answer.

(d) Suppose  $f'(5) = 3$  and  $f''(x) < 0$  for all  $x$  in the closed interval  $5 \leq x \leq 8$ . Use the line tangent to the graph of  $f$  at  $x = 5$  to show that  $f(7) \leq 4$ . Use the secant line for the graph of  $f$  on  $5 \leq x \leq 8$  to show that  $f(7) \geq \frac{4}{3}$ .

9. 2008AB4 [non-calculator]

The functions  $f$  and  $g$  are given by  $f(x) = \int_0^{3x} \sqrt{4+t^2} dt$  and  $g(x) = f(\sin x)$ .

(a) Find  $f'(x)$  and  $g'(x)$ .

(b) Write an equation for the line tangent to the graph of  $y = g(x)$  at  $x = \pi$ .